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The Effect of Heating Rates on Low Temperature Hexane Air Combustion

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Abstract

Combustion of hydrocarbon fuels is traditionally separated into slow reaction, cool flame, and ignition regimes based on pressure and temperature. Standard tests, such as the ASTM E659, are used to determine the lowest temperature required to ignite a specific fuel mixed with air at atmospheric pressure. It is expected that the initial pressure and the rate at which the mixture is heated also influences the limiting temperature and the type of combustion. This study investigates the effect of heating rate, between 4 and 15 K/min, and initial pressure, in the range of 25 to 100 kPa, on ignition of *n*-hexane air mixtures. Mixtures with equivalence ratio ranging from $\Phi = 0.6$ to $\Phi = 1.2$ were investigated. The problem is also modeled computationally using an extension of Semenov's classical autoignition theory with a detailed chemical mechanism. Experiments and simulations both show that in the same reactor either a slow reaction or an ignition event can take place depending on the heating rate. Analysis of the detailed chemistry demonstrates that a mixture which approaches the ignition region slowly undergoes a significant modification of its composition. This change in composition induces a progressive shift of the explosion limit until the mixture is no longer flammable. A mixture that approaches the ignition region sufficiently rapidly undergoes only a moderate amount of thermal decomposition and explodes quite violently.

Keywords: n-hexane oxidation, direct absorption, heating rate

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1. Introduction

Ignition of fuel in the fuel tank or surrounding flammable leakage zones is one of the main safety concerns for the commercial aviation industry. The presence of hot surfaces is unavoidable in aircraft. Consequently, ignition by hot surfaces close to the autoignition temperature is particularly relevant to design of fuel handling systems and analysis of hazards in aviation and industrial settings. While the ASTM E659 is a standard test for autoignition temperature, only the minimum temperature for ignition at atmospheric pressure is determined [1, 2] for a particular geometry and size. The specific mixture composition is neither controlled nor measured since the liquid test fuel is injected into a heated open vessel. The contents are not actively mixed and it is presumed that a considerable range of composition exists within pockets of gas in the vessel as evaporation of liquid fuel occurs [3]. It can also be expected that numerous parameters, including the pressure, the composition, the size and shape of the vessel, and the rate at which the mixture is heated, will influence the limiting temperature and the type of combustion event. In prior laboratory research, the combustion products have either been condensed and the liquid analyzed later [4], or a gas chromatograph was used to analyze a small sample at a maximum frequency of about 0.1 Hz [5]. Additional work was done in rapid compression machines at higher temperatures (600 K - 800 K) [6] and gas sampling techniques [7, 8]. While pressure transients are easily captured in these experiments, fast and accurate fuel concentration measurements requiring optical techniques have never previously been applied to the autoignition phenomenon.

The objective of this study is to investigate the effects of heating rate, composition, and initial pressure on the thermal ignition processes that can occur when hydrocarbon fuels come in contact with heated elements by using an experimental setup that allows for precise control of the gas composition and temperature, and a fast measurement rate of the fuel content. Hexane was selected as a test fuel. It has a similar autoignition temperature (498 K [9, 10]) to kerosene and is comparable to jet fuel (511 K turbine fuel [11], Jet A [2]). Hexane is easy to handle in liquid form but vaporizes readily, and detailed chemical reaction mechanisms are available. In the following section, the experimental setup and the modeling approach are described. Then, the experimental results are presented. Finally, the results are interpreted based on an extension of Semenov's classical autoignition theory with a detailed chemical mechanism.

2. Experimental Setup and Modeling Approach

2.1. Experimental Setup

The test vessel (Figure 1) is a closed 400 mL Pyrex cell (surface to volume ratio $\approx 0.85 \text{ cm}^{-1}$). Prior to experiments, the test cell is evacuated to less than 10 Pa. The vessel is filled with *n*-hexane, nitrogen, and oxygen using the partial pressure method, then thoroughly mixed by a circulation pump. Hexane is injected as a liquid through a septum at a partial pressure below its vapor pressure in order to ensure complete vaporization. The uncertainty in composition is ± 0.01 kPa for each species, due to the accuracy of the pressure measurement. Two sapphire windows are spaced 9 cm apart, providing optical access for the laser measurement. The vessel is suspended inside an aluminum shell with an air gap of approximately 3 mm, and the shell is heated by two band heaters rated at a total of 800 W. The temperature inside the vessel is measured by a K-type thermocouple that has been coated with silica in order to avoid catalytic effects. During the experiment, transient pressure is measured with a separate fast-response static pressure gage (> 10 kHz). The final heating rate is computed from the pressure measurements using the values before the onset of the reaction, i.e. assuming no change in moles, using

$$\frac{dT}{dt} = \frac{V}{n\tilde{R}}\frac{dP}{dt} \tag{1}$$

because the response time of the pressure transducer is much shorter than that of the thermocouple. The data is directly analyzed and averaged giving an effective sampling rate of 8 Hz. Experiments were performed at three total pressures: 26, 67, and 101 kPa, three equivalence ratios, Φ : 0.6, 1, and 1.2, and heating rates between 4 K/min and 14 K/min.

The fuel concentration is measured by direct absorption [12, 13]. A commercially available 3.39 μ m HeNe laser is passed through a chopper running at 300 Hz. The beam is split two ways before entering the test cell through a 0.5 mm thin sapphire window. The main beam is passed through the test cell and measured by a detector on the other side, while the second beam is sent to a reference detector to correct for variations in the initial laser intensity. High angles of incidence (~ 10°) were used to avoid intensity changes due to interference effects from the windows caused by thermal expansion since internal reflections are scattered through a wider angle.

The n-hexane mole fraction is calculated from the detected laser transmission using Beer's law. The C-H bond in any hydrocarbon molecule absorbs around the 3.39 μ m wavelength, so changes from *n*-hexane into other hydrocarbon molecules cannot be detected. Thus an equivalent *n*-hexane mole fraction, $X_{C_6H_{14}}^*$, is calculated based on the absorption cross section of *n*-hexane, which is found through separate calibration experiments to be $\sigma_{\nu} = 38 \pm 1 \text{ m}^2/\text{mole}$. This value is in agreement with values from the literature (Jaynes and Beam found 45 m²/mole [14], Drallmeier 38.5 ± 2 m²/mole [13, 12], Tsuboi et al. $36.2 \pm 7 \text{ m}^2/\text{mole}$ [15, 12], Mevel et al. $39.92 \pm 2 \text{ m}^2/\text{mole}$ [34]). The intensity changes are converted to equivalent mole fractions using the intensity measurements:

$$\frac{I}{I_0} = \exp\left(-\frac{\sigma_{\nu} P_{fuel} L}{\tilde{R}T}\right) \tag{2}$$

$$X_{C_6H_{14}}^* = \frac{P_{fuel}}{P_{total}} = \frac{\tilde{R}T}{\sigma_{\nu}LP_{total}} \left[\ln\left(\frac{I_1(t)}{I_2(t)}\right) - \ln\left(\frac{I_1^0}{I_2^0}\right) \right]$$
(3)

2.2. Modeling Approach

The experiment is modeled using Semenov's theory [16] for thermal ignition, assuming a well stirred constant volume reactor filled with a uniform mixture of *n*-hexane in air. The wall temperature is increased from room temperature at a constant rate, α , which is included in the energy equation as: $T_w = T_w^0 + \alpha t$. The temperature variation with time is computed from the energy conservation equation:

$$V\rho c_v \frac{dT}{dt} = V \sum_{i=1}^k \dot{\omega}_i u_i + Sh\left(T_w^0 + \alpha t - T\right) = \dot{q}_r + \dot{q}_w.$$

$$\tag{4}$$

The species variation with time is computed with the mass conservation equation

$$\frac{dY_i}{dt} = \frac{W_i \dot{\omega}_i}{\rho}, i = 1, 2, \dots, k \tag{5}$$

where k is the total number of species. The vessel volume, V, and surface area, S, are constant while the density, ρ , and specific heat at constant volume, c_v , are calculated at each solver time step. The heat transfer is modeled with Newton's law of cooling using a lumped parameter, h, to approximate free convection inside the vessel. The change in temperature is determined by the competition between the chemical heat release, \dot{q}_r , and the heat loss rate, \dot{q}_w , into which the terms of the energy equation have been grouped. Cantera [17] is used to compute the net chemical production rate, $\dot{\omega}_i$, utilizing a detailed chemistry mechanism, as well as all thermodynamic properties for both individual species, such as the internal energy u_i , and the gas mixture as a whole. A variable-coefficient ODE solver (VODE) is used to integrate the system of equations [18].

The basis for our reaction mechanism is the detailed model of Ramirez et al. [19]. This kinetic scheme was developed to model decane and biofuel chemistry. Further validation for *n*-hexane was necessary for the present study; this is presented along with the modeling results. The mixture is initialized at a given pressure, temperature, and equivalence ratio, and then the energy equation is integrated forward in time with the wall temperature rising at a specified rate, α .

3. Experimental Results

Experiments were performed varying the composition, initial pressure, and heating rate applied to the vessel walls. Figures 2 and 3 show the temperature, pressure, and fuel mole fraction during two representative experiments performed with a slightly fuel rich mixture ($\Phi = 1.2, 2.6 \%$ *n*-hexane in air) and at an initial pressure of 101 kPa. The mixture of Fig. 2 was heated at a rate of 4.25 K/min and underwent a slow reaction. A slow reaction case is characterized by a slow consumption of the fuel with a minimal pressure rise. The mixture of Fig. 3 was heated at 11 K/min and underwent ignition. In this context, an event characterized by rapid consumption of the fuel accompanied by a large pressure rise will be referred to as either an ignition case or fast reaction case.

The slow reaction case (Fig. 2) has several features that make it significantly different from the ignition case. As the temperature increases from room temperature, we observe a slow consumption of the fuel (C-H bonds) starting at 500 K (2500 s), which reduces the fuel concentration from 2.6% to 0.45% over 250 s until the heating system is turned off at 540 K. During this time neither the pressure nor the temperature rises above the trajectory prescribed by the input heating rate.

The temperature and pressure plot show small steps in the ramp from room temperature to 540 K. These steps are due to the response time of the controller and the aluminum shell to the overall heating rate and temperature change during the initial fuel consumption is 4.25 K/min. Heating the same mixture ($\Phi = 1.2$) at roughly twice the heating rate, 11 K/min, results in a fast reaction (Fig. 3). Upon ignition, we observe a spike in pressure, reaching a peak of 330 kPa with elevated pressure for 0.5 seconds. The temperature peak is visible but substantially smaller due to the much slower response time of the thermocouple as compared to the pressure transducer.

From the changes in the fuel concentration, temperature, and pressure measurements, we observe that the fast reaction occurs at 1010 s. At this time, we estimate the temperature in the vessel to be 473 K (200 °C), whereas the thermocouple reads 400 K. Due to the limited response rate of the thermocouple, discussed earlier, the actual gas temperature must be inferred from the pressure measurements, assuming the mixture is an ideal gas and negligible changes in the number of moles. At 1000 s we see an initial decrease in fuel concentration followed by a rapid consumption of the fuel during the ignition transient at ~1010 s. Unlike the slow reaction, in this case the response of the measurement system is limited by signal contamination from light emission during the ignition.

The effect of initial pressure and composition was examined for 14 conditions and the outcomes are shown in Figure 4. The following changes in the experimental conditions transition the system from a slow reaction case to an ignition case: (1) increasing the pressure (between 26 kPa - 100 kPa), (2) increasing the heating rate (4 - 12 K/min), (3) increasing the equivalence ratio in the region investigated ($\Phi = 0.6 - 1.25$). Each of these factors is confirmed experimentally, while keeping the other two parameters constant.

4. Modeling

In order to model this system, a detailed kinetic scheme had to be identified and validated against appropriate low temperature data. Although hydrocarbons have been widely studied, there exists little data concerning n-hexane oxidation [20]. Curran et al. [21] studied hexane isomer chemistry through the modeling and measurement of exhaust gases from an engine. Shock tube experiments have been performed by Burcat et al. [22] and Zhukov et al. [23]. Kelley et al. [24] recently reported laminar flame speeds for C-5 to C-8 n-alkanes. To our knowledge, no low temperature experimental data exists for n-hexane-oxygen mixtures. It should also be noted that no single detailed kinetic scheme is available to model n-hexane combustion chemistry from low to high temperature. In order to describe the kinetics of n-hexane-air mixtures, we employed the C-7 basis of the detailed model published by Ramirez et al. [19] which includes n-hexane.

4.1. Kinetic scheme validation

For validation at high temperature, we used the experimental data of Burcat et al. and Zhukov et al. For validation at intermediate and low temperature, we used n-heptane flow reactor and jet stirred reactor data from Held et al. [25] and Dagaut et al. [26], respectively.

The experimental *n*-hexane-oxygen-diluent mixture auto-ignition delay times from Burcat et al. [22] and Zhukov et al. [23] are compared in Fig. 5 to the predictions of the Ramirez model. The computed delay times are in reasonable agreement with the experimental results. Although the model typically underestimates the results of Burcat in the high temperature range, the mean relative error does not exceed 30%. The mean error with respect to the data of Zhukov is around 25%. Considering the usual uncertainty of 20% associated with shock-tube delay times, the model reproduces the experimental data adequately for the purpose of the present study.

The flow reactor experimental data from Held et al. [25] are compared in Fig. 6 (a) to the model predictions for a lean n-heptane-oxygen-nitrogen mixture. The temporal mole fraction profiles of the main species are relatively well predicted. The consumption of both reactants, C_7H_{16} and O_2 , are satisfactorily predicted throughout the experiment, whereas the production of CH_4 and C_2H_4 are overestimated early in the oxidation process, and CO mole fraction is underestimated. It should also be noted that the temperature profiles (not shown) are in good agreement with experiments.

The jet-stirred reactor experimental data from Dagaut et al. and the model predictions are compared in Fig. 6 (b) for a stoichiometric n-heptaneoxygen-nitrogen mixture. The CO mole fraction is well predicted everywhere except within the the region with a negative temperature coefficient (NTC), where an increase in temperature leads to longer induction times (700 - 800 K). The CO₂ mole fraction is underestimated in the low temperature range, but is in close agreement in the high temperature range. The CH₄ mole fraction is overestimated almost throughout the temperature range. Finally, it can be noted that the NTC region position is correctly predicted.

The last experimental datum to be modeled in testing the validity of the detailed kinetic scheme is the auto-ignition temperature. The experimental value is near 500 K for a stoichiometric n-hexane-air mixture at atmospheric

pressure. The predicted temperature, based on a constant-volume reactor simulation, is 540 K.

Although the model is not able to reproduce the whole set of selected experimental data with good accuracy, the general trends of *n*-hexane-oxygen mixture reactivity are predicted. A better agreement might be obtained by adjusting the dominant kinetic parameters. However, this would require additional experimental data and is beyond the scope of the present study.

4.2. Fast and slow combustion modeling

The purpose of the modeling study was to determine if an existing reaction mechanism could qualitatively reproduce the observed trends using a simple reactor model that simulates the key features of the present experimental set-up. The reactor was modeled as a homogenous mixture in a closed, fixed volume with a specified wall temperature that is a function of time. Heat transfer from the vessel wall to the contents is characterized thorough the wall heat transfer coefficient, h, with a value of 15 W/(m² K). The value of the heat transfer coefficient was determined iteratively until the switch between the slow and fast reaction was observed for heating rates of 5 and 10 K/min and is consistent with heat transfer from free convection of gases [27].

Figures 7 and 8 present the simulation results for a slow reaction and an ignition event corresponding to a rich mixture, $\Phi = 1.2$, with heating rates of 5 and 10 K/min, respectively. In the case of the slow reaction, a slight increase in temperature and pressure can be seen around 2900 s. This time corresponds to the maximum rate of *n*-hexane and oxygen consumption. The reactant consumption extends over a long period of time, several hundred seconds. Although the mixture is rich, only 75 % of the oxygen is consumed after 3100 s. In the case of the ignition event, a sharp increase in temperature and pressure is observed at about 1500 s. At this time, the reactants are consumed and products are formed over a short period of time, on the order of tens of milliseconds. Figures 7 and 8 demonstrate that reactant consumption proceeds at essentially constant temperature and pressure in the case of a fast combustion event.

It is remarkable that a variation of a factor of two in the heating rate results in a completely different mode of combustion in these two cases. Further the temperature at which strong reactant consumption occurs is actually lower in the higher heating rate case (473 K) than in the lower heating case (500 K).

4.3. Heat production and losses

In order to help understand the differences between the slow reaction and ignition cases, the heat production and loss rates have been calculated, along with the energy release rate for each elementary reaction (Figures 9 and 10).

The heat release term, \dot{q}_r , and the magnitude of the heat loss term, $|\dot{q}_w|$, from Equation 4, are shown in Figure 9 (note that the time axes are scaled so that temperature history will coincide in the absence of chemical reactions). The initial value of the heat loss term corresponds directly to the heating rate to the reactor. The inset shows the slight lag of the heat loss term in comparison to the heat release term. For the slow reaction case the difference diminishes as the reaction becomes less exothermic, while for the ignition case the difference increases as mixture move towards the ignition point. In the slow reaction case, the chemical heat release is balanced by heat loss at the wall. In the ignition case, the energy release exceeds the heat loss at the wall by several orders of magnitude when ignition occurs. The energy release by the chemical reactions is ~ 10⁷ times greater during an ignition case than during the slow reaction case. The difference in chemical reaction pathways is shown by the fact that the slow reaction heat release peaks before the ignition case does.

The chemical reactions producing and consuming heat are very different (Fig. 10) for the slow and fast reaction cases. In the slow reaction case, the reactions that release energy involve weakly reactive species such as HO_2 , H_2O_2 , and alkylperoxides. Although most of these reactions are highly exothermic, they proceed at a slow rate, keeping the energy release rate low. In the ignition case, the energy release is driven by two reactions: $H + OH + M \iff H_2O + M$ and $CO + OH \iff CO_2 + H$. These reactions produce the two main reaction products, H_2O and CO_2 , and are very exothermic.

4.4. Reaction pathway analysis

The previous analyses demonstrates that the heating rate of the reactor controls the thermodynamic conditions which in turn control the chemical pathways. The dominant chemical pathways for each case are analyzed via detailed species rate of production and reaction pathway diagrams.

4.4.1. Radicals and atoms rate of production

Rate of production analysis have been performed for O and H atoms, as well as, OH and HO₂ radicals. Figure 11 presents the results obtained for both the slow reaction and the ignition cases for H and OH. The dominant reaction responsible for the consumption of the H atoms during the slow reaction process is: $H + O_2$ (+M) $\iff HO_2$ (+M), forming less reactive HO₂ radicals. Conversely, during the ignition process, H atoms are primarily consumed through the $H + O_2 \iff OH + O$ reaction, producing OH radicals.

In the slow reaction case, OH radicals are produced by OH elimination reactions and are mainly consumed by the following reactions:

- (i) $CH_2O + OH \iff HCO + H_2O$
- (ii) $H_2O_2 + CO + OH \iff HOCHO + HO_2$
- (iii) $CH_3HCO + OH \iff CH_3CO + H_2O$
- (iv) $C_6H_{14} + OH \iff cC_6H_{13} + H_2O.$

where cC_6H_{13} corresponds the to 3-hexyl radical. The analysis shows that no branching process occurs.

In the ignition case, OH radicals are rapidly produced by the following branching reactions:

- (i) $H + O_2 \iff OH + O$
- (ii) $O + H_2 \iff OH + H$
- (iii) $H_2O + O \iff OH + OH$

and are consumed by the following exothermic reactions:

- (i) $H + OH (+M) \iff H_2O (+M)$
- (ii) $H_2 + OH \iff H_2O + H$
- (iii) $CO + OH \iff CO_2 + H$

The last two reactions also regenerate H atoms.

The consumption of HO_2 radicals is driven by reactions which produce non-reactive species, mainly H_2O_2 . In the fast reaction case, their consumption is driven by the $H + HO_2 \iff OH + OH$ reaction, which produces the very reactive OH radicals. Finally the O atoms take part in the chain branching process: $H + O_2 \iff OH + O$ and $O + H_2 \iff OH + H$, but only during the ignition event and not during the slow reaction.

4.4.2. Reaction pathway diagrams

A 10% threshold is used for the element flux pathway diagrams in order to underline the most important pathways for both cases. The carbon element pathways for the two phases in the oxidation process are summarized in Figures 12 and 13. The first phase corresponds to the period where the temperature increases from 500 to 540 K. In the slow reaction case, this period extends from 2350 to 2850 s; for the fast reaction case, it extends from 1220 to 1430 s. As shown in Figure 12 the main path for *n*-hexane consumption in both cases is the following:

- (i) H abstraction by OH from the third carbon atom (C3),
- (ii) O_2 addition on carbon C3,
- (iii) intramolecular H abstraction by O_2 from the fifth carbon atom (C5),
- (iv) second O_2 addition on carbon C5,
- (v) OH elimination-intramolecular H abstraction by O_2 on carbon C3cetone formation on carbon C3.

During the slow reaction, a significant amount of the 5-hydroperoxy-hexan-3-one is decomposed into OH, CH_3HCO , and $C_2H_5COCH_2$. The last species is further converted through a series of reactions ultimately leading to CH_2O and C_2H_5O . During the first phase, these reaction rates are almost an order of magnitude higher in the slow reaction case as compared to the ignition case. This is explained by the significantly longer time the mixture spends under these conditions, allowing for an increase in OH concentration, and thus increasing the initiation rate.

During the second phase, additional pathways appear to be important. These are presented in Figure 13. For the slow reaction case, this phase extends from 2870 and 3100 s with an increase of temperature of 20 K to reach 560 K. This phase is mainly characterized by successive:

- (i) CO or CO_2 elimination
- (ii) O_2 addition
- (iii) H addition
- (iv) OH elimination

The overall reaction rate remains the same throughout the entire process $(\sim 10^{-5} \text{ kmol}/(\text{m}^3 \text{ s}))$ and, at 3100 s, 95% of the initial *n*-hexane content is consumed.

For the fast reaction case, the second phase extends from 1430 to 1495 s, at which point ignition occurs, with an increase of temperature until 790 K. The reaction rates are on ~100 times higher than the reaction rates of the slow reaction case in this phase. During this phase, C-C bond rupture is favored over O_2 addition. This process rapidly forms CO which then reacts with OH radicals to form CO_2 and H atoms. This fast production of H atoms, further sustained by the temperature increase, induces an increase in the overall reaction rate through the chain branching reaction $H + O_2 \iff$ OH + O, and drives the ignition of the mixture. A large amount of O_2 is consumed through addition reactions during the slow reaction. During the fast reaction case, O_2 is still available in the gas phase for the branching process.

4.5. Explosion Limits

Figure 14 shows the simulated thermodynamic state trajectories, for the case with $\Phi = 1.2$, along with the experimental explosion limits obtained for a 2.7% *n*-hexane in air by Towsend et al. [28]. Figure 14 (a) illustrates the temporal evolution whereas Figure 14 (b) emphasizes the *n*-hexane concentration evolution. As shown in Figure 14 (a), in the slow reaction case the mixture spends a proportionally long time, several hundred seconds, at a temperature slightly below the auto-ignition temperature 498 K. Due to the extended period the mixture spends at a temperature close to the auto-ignition temperature, more than 50% of reactants are consumed before entering the explosion region. This is shown in Figure 14 (b). Both Figures together show the importance of considering the evolution, in time and reaction progress, of a particular mixture rather than a simplified threshold point of view.

Analysis of the chemical composition during the slow reaction case shows that mixtures changes significantly from the original $\Phi = 1.2$ (2.6%) *n*-hexane air mixtures into a mix of other hydrocarbons, mainly oxygenated hydrocarbons. The ignition behavior of this mixture is no longer characterized by the explosion limit of the 2.7% *n*-hexane air mixtures and no ignition is observed as the mixtures enters this ignition region. A slight acceleration of the reaction rate is observed just at the entrance of the explosion region. However, the energy release rate remains too low for ignition to occur and is balanced by the heat losses at the wall.

Conversely, the fast reaction case progresses much more rapidly, and the mixture quickly enters into the explosion region. In the fast reaction case, although a significant fraction of the reactants, around 10%, is consumed before the mixture enters the explosion region, the composition is not modified

enough to avoid explosion and the reactants consumption occurs according to a fast reaction driven by chain branching reactions.

Given the configuration of the experiment, the system has an intrinsic thermochemical feedback loop. By that we mean the dynamics of the system are controlled by the coupling of the thermodynamic state and the chemical kinetics. Depending on the heating rate, diverging chemical paths occur and in turn influence the evolution thermodynamic state.

5. Concluding Remarks

In the classical view of autoignition, a minimum temperature exists that leads to the ignition of a given fuel under specified conditions. It is known that the autoignition temperature depends on many parameters and the present study demonstrates that one of these, the rate at which the mixture is heated, greatly influences how the reaction progresses, and consequently whether the mixture ignites. Further, in some of the situations we have examined, we find that it is possible to consume all the fuel without an ignition event at a well-defined temperature.

For instance, increasing the heating rate of the vessel by a factor of 2, from 4.25 to 11 K/min, produces an ignition event with a rapid pressure rise in a mixture that otherwise would have generated a slow reaction with no significant pressure rise. The same transition in behavior is shown for an increase in equivalence ratio from 1 to 1.2. In the range investigated, the minimum heating rate required for fast reactions decreases with increasing equivalence ratios.

The computations demonstrate that a model based on Semenov theory is capable of capturing the qualitative behavior of the oxidation event. By adding the heating rate, α , to the classical Semenov model, we are able to reproduce the observed transition from a slow reaction case to an ignition case with increasing heating rate; with the necessity of determining the lumped heat transfer coefficient empirically.

The type of reaction that the mixture undergoes is a complex function of the mixture composition, thermochemical feedback loop, residence time, and heat transfer. Consequently, for sufficiently slow heating rates it is possible for the fuel to be completely consumed without any rapid pressure transient at temperatures above the classical autoignition value. The experimental results also indicate that the transitional heating rate is a function of the initial pressure and composition. The results presented here show that an assessment of safety should include factors such as the temperature, pressure, mixture composition, and heating rate rather than just a threshold temperature when considering autoignition. For instance, the temperatures at which the reactions occur are near the listed autoignition temperatures for the slow reaction case, but slightly below for the ignition case. These factors come into play both when designing a standard test procedure to determine fuel properties as well as assessing the safety of a particular engineering design.

The simulations show that the slow reaction and ignition behavior can be modeled correctly, however due to the complex chemical pathways and limited data on fuels like *n*-hexane at low temperatures it is difficult do predict the temperature at the onset of reaction to an accuracy better than 50 K.

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Appendix: Oxygen concentration measurements

Introduction

In addition to the fuel concentration measurements, an attempt has been made to spectroscopically monitor the molecular oxygen concentration during the heating rate experiments. Since transitions in the A band near 760 nm are spin forbidden, direct absorption measurements of O_2 is complicated due to the very weak absorption cross sections [29]. One method for overcoming this limitation is the use of a derivative technique of spectroscopy with second harmonic (2f) detection as demonstrated by Kroll et al. [30], Philippe and Hanson [29], and Rieker and Hanson [31]. The 2f technique utilizes a high frequency modulation of the output wavelength of a laser diode as its wavelength is scanned across the absorption line.

First, the basic principles of the technique are explained. Second, the experimental setup is described. Third, the calibration procedure is presented. Finally, the experimental results are detailed.

Basic principles

A comprehensive description of the laser diode wavelength-modulation spectroscopy technique with second harmonic detection can be found in [32]. Only the main steps are highlighted in the following.

The attenuation of a laser beam's intensity, $I(\nu)$, as it travels through an absorbing medium is described by the Beer-Lambert law:

$$I(\nu) = I_0(\nu) \exp(-\alpha(\nu)L), \tag{6}$$

where $I_0(\nu)$ is the incident laser beam intensity, $\alpha(\nu)$ is the absorption coefficient, L is the path length and ν is the light frequency.

For weak absorption coefficients, the Beer-Lambert law can be approximated by:

$$I(\nu) \approx I_0(\nu)(1 - \alpha(\nu)L)). \tag{7}$$

Applying a modulation of frequency ω to the diode input current induces the modulation of the diode output light wavelength such that:

$$\nu(t) = \bar{\nu} + a\cos(\omega t),\tag{8}$$

where t is the time, $\bar{\nu}$ the mean frequency and a the modulation amplitude.

A carrier signal with a low frequency relative to the modulation frequency is added to the modulation signal in order to scan across the absorption line. For carrier signal with low amplitude, the incident laser beam intensity variations are small. The transmitted light intensity can thus be written as:

$$I(\nu) = I_0 \left[1 - \alpha \left(\bar{\nu} + a \cos(\omega t) \right) L \right].$$
(9)

Expanding the time dependent part in a Taylor series and collecting the terms of same frequency gives the following expression as formulated by Reid and Labrie [33]:

$$\alpha(\bar{\nu} + a\cos(\omega t)) = \sum_{n=0}^{\infty} H_n(\bar{\nu})\cos(n\omega t), \qquad (10)$$

where:

$$H_n(\bar{\nu}) = \frac{2^{1-n}}{n!} \alpha^n \frac{d^n \alpha(\nu)}{d\nu^n}_{\nu=\bar{\nu}}, n \ge 1,$$
(11)

with *n* the harmonic order. A lock-in amplifier can then be used to selectively amplify the second harmonic term. Assuming a Lorentzian line shape for the absorption line and evaluating at $\nu = \nu_0 = \bar{\nu}$, the second derivative of the absorption coefficient can be expressed as:

$$\left. \frac{d^2 \alpha(\nu)}{d\nu^2} \right|_{\nu=\nu_0=\bar{\nu}} = -\frac{2\alpha_0}{\Delta\nu^2}.$$
(12)

For a prefect gas, the second derivative of the signal intensity can be linked to the oxygen partial pressure by the following:

$$\frac{d^2 I}{d\nu^2}\Big|_{\nu=\nu_0=\tilde{\nu}} = \frac{2I_0 L \sigma_{\nu}}{RT \Delta \nu^2} P_{O2} \exp\left(-\frac{\sigma_{\nu} L}{RT} P_{O2}\right) = C_1 P_{O2} \exp(-C_2 P_{O2}), \quad (13)$$

where σ_{ν} is the absorption cross section, C_1 and C_2 are constants obtained through a calibration procedure.

Experimental setup and calibration procedure

The experimental arrangement is shown in Figure 15. It consists of a signal generator, a summing amplifier, a laser diode with current and temperature controllers, a lock-in amplifier, a low noise preamplifier with bandpass filter, and a waveform recorder. The signal generator is used to create a sawtooth-like carrier signal with a frequency of 80 Hz and an amplitude of ~ 100 mA. This signal scans across the absorption line. The second signal, the sine wave, is generated by the lock-in amplifier's internal signal generator with a

frequency of 23.5 kHz and an amplitude of 4 mA. These signals are summed and then sent to the laser diode current controller. Both the sine wave signal and the transmitted laser diode beam are collected by the lock-in detector. The resulting signal is then filtered and recorded by the waveform recorder.

The height of the 2f peak is calibrated against the partial pressure of oxygen. Figure 16 shows that the peak height varies linearly with the amount of oxygen as predicted from Equation 13 for the range of oxygen concentrations investigated. For calibration, the vessel is first evacuated to below 10 Pa and then filled with increasing amounts of oxygen. The second calibration was performed by first filling the vessel with 67 kPa of N₂ and then mixing the oxygen with the nitrogen in increasing steps. The linear constant is reduced when nitrogen is added, which is expected due to the effect of pressure broadening. Also indicated in Figure 16 is the uncertainty in the calibration measurement. This uncertainty is strictly based on the evaluation of the standard deviation about the mean of the time series data acquired over the measurement interval, typically 30 seconds. The uncertainty in the pressure is less than the indicated symbol size. The calibration was performed at room temperature.

Application to oxygen measurements

The measurement of oxygen concentration was only implemented successfully once during the course of this investigation. The experimental technique has proven to be extremely sensitive the variations in the optical path. The experimental procedure of heating the vessel from room temperature over a very long time period causes the glass vessel to expand. This produces both an etalon effect and beam steering, which we were only able to correct for by using a non-reactive mixture for one data set. Figure 17 shows the consumption of the oxygen and fuel for a fuel rich mixture ($\Phi = 1.2$) at a low initial pressure ($P_0 = 26.67$ kPa) heated at a 11.2 K/min. The measurements show consumption of the fuel and oxygen at the same time, which agrees with the simulation results of the slow reaction shown in Figure 8 (a). This result agrees with the overall trends shown in Figure 4, which show that reducing pressure, heating rate, or equivalence ratio sufficiently in the range investigated leads to a slow reaction of the mixture instead of ignition.

For future experiments, the limitations shown here could be addressed in several ways. First, the impact of the optical path variations could be reduced by increasing the test cell dimension or isolating the windows mechanically from the test cell. Additionally, the sensitivity of the measurements could be increased by evacuating or nitrogen flushing the laser beam path outside the test cell, which would avoid perturbations due the oxygen contained in air. Finally, the overall experimental procedure could be adapted to start the temperature ramp at a higher temperature, reducing the total temperature change.

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Figure 1: Schematic of the experimental set-up (all dimensions are in cm)



Figure 2: Slow reaction of a fuel rich ($\Phi = 1.2$) *n*-hexane/air mixture at an initial pressure of 101 kPa heated at 4.25 K per minute



Figure 3: Ignition of a fuel rich ($\Phi = 1.2$) *n*-hexane/air mixture at an initial pressure of 101 kPa heated at 11 K per minute



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Figure 5: Comparison of shock tube experimental data to the predictions of the Ramirez model for n-hexane-oxygen-argon mixture. (a) data of Burcat et al. [22] (b) data of Zhukov et al. [23]



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Figure 7: Simulated temperature and pressure profiles for a *n*-hexane-air mixture for two different heating rates. Conditions: $\Phi = 1.2$ (a) $\alpha = 5$ K/min (b) $\alpha = 10$ K/min



Figure 8: Simulated species profiles for a *n*-hexane-air mixture for two different heating rates. Conditions: $\Phi = 1.2$ (a) $\alpha = 5$ K/min (b) $\alpha = 10$ K/min



Figure 9: Chemical heat production and heat loss rates for a *n*-hexane-air mixture for two different heating rates. Conditions: $\Phi = 1.2$; $\alpha = 5$ K/min and $\alpha = 10$ K/min (Ignition - Ign, Slow Reaction - SR)



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Figure 11: Rate of production of H atoms and OH radicals for a $\Phi = 1.2$ *n*-hexane-air mixture and two different heating rates: (a) and (b), $\alpha = 5$ K/min; (c) and (d), $\alpha = 10$ K/min



Figure 12: Carbon reaction pathways during the first phase of a *n*-hexane-air mixture oxidation for two heating rates. Conditions: $\Phi = 1.2$; $\alpha = 5$ and 10 K/min. Black arrows: common pathways. Blue arrows: additional pathways observed during the slow reaction. The first phase extends from 2350 to 2850 s for the slow reaction and from 1220 to 1430 s for the fast reaction.



Figure 13: Carbon reaction pathways during the second phase of a n-hexane-air mixture oxidation for two heating rates. The second phase extends from 2850 to 3100 s for the slow reaction and from from 1430 to 1495 s for the fast reaction.



(b)

Figure 14: Thermodynamic state trajectories along with the explosion limits [28] for a *n*-hexane-air mixture with different heating rates. Conditions: $\Phi = 1.2$; $\alpha = 5$ and 10 K/min; (a): temporal evolution (500 s elapsed time between points). (b): *n*-hexane percentage consumed in the boxed region of (a).



Figure 15: Schematic of the experimental setup for molecular oxygen measurements



Figure 16: Calibration curve, second harmonic peak height as a function of molecular oxygen partial pressure with $\pm \sigma$ uncertainty bars (O₂ only and O₂ with 67 kPa N₂ dilution)



Figure 17: Measurement of the molecular oxygen and fuel concentration during a slow reaction for a *n*-hexane/air mixture. Conditions: $P_0 = 26.67$ kPa, $\Phi = 1.2$, $\alpha = 11.2$ K/min